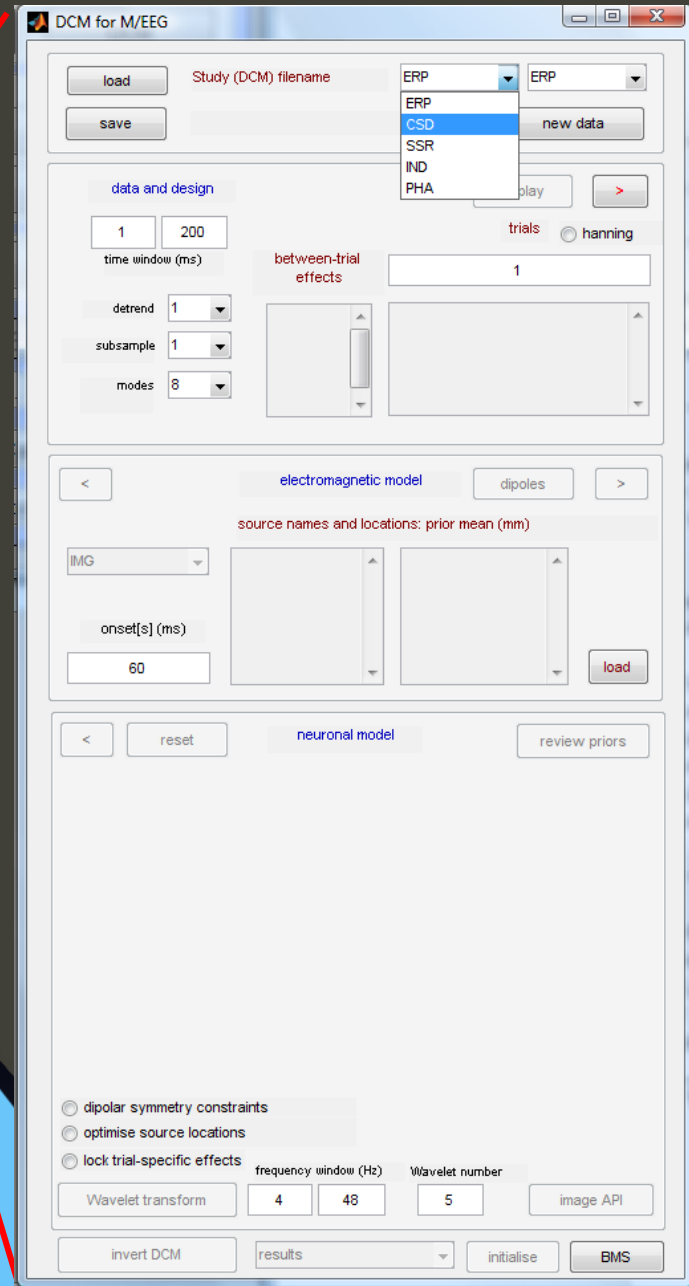
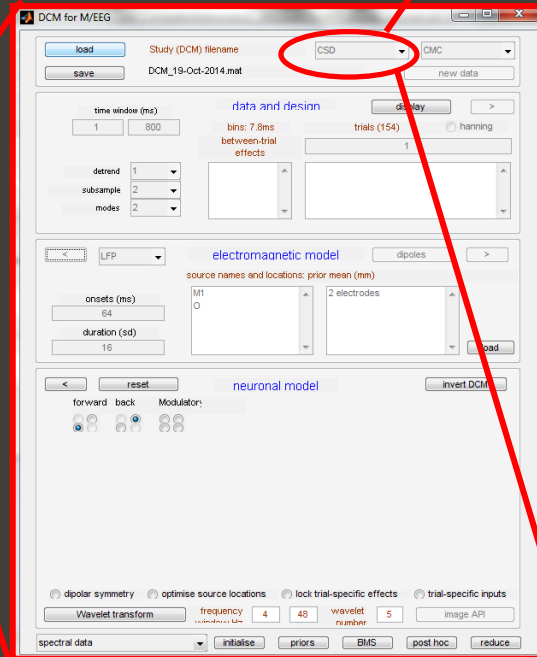
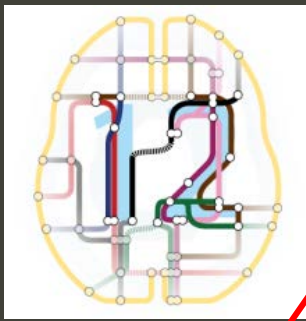


Dimitris Pinotsis
City—University of London &
MIT
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Dynamic Causal Modelling for Steady State Responses

- ✓ Similar statistical features
- ✓ Summarize activity in a compact way
- ✓ Quantitative description in terms of a **characteristic frequency**
- ✓ Cannot describe nonlinear frequency coupling (DCM for IR)
- ✓ Changes oscillatory power and coherence may not yield information directly (DCM for SSR)

In SPM



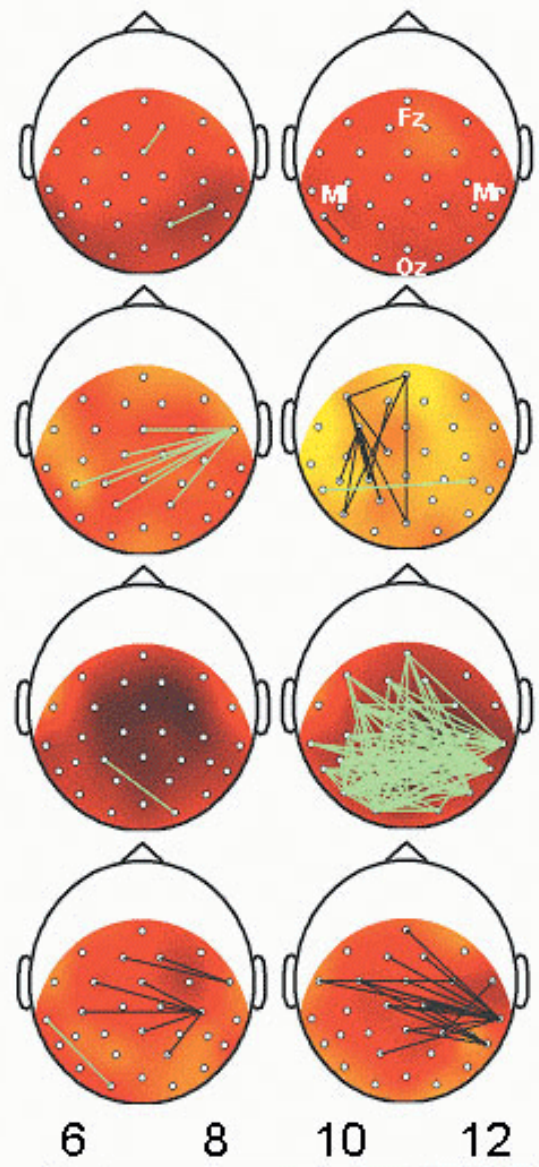
- ✓ Perception, attention, memory, executive control
- ✓ Highly parallel processing by the brain
- ✓ Information transfer
- ✓ Synchronized neuronal discharges
- ✓ Select relevant information



'Mooney' faces

Significant phase locking
Significant phase scattering

No Perception Perception



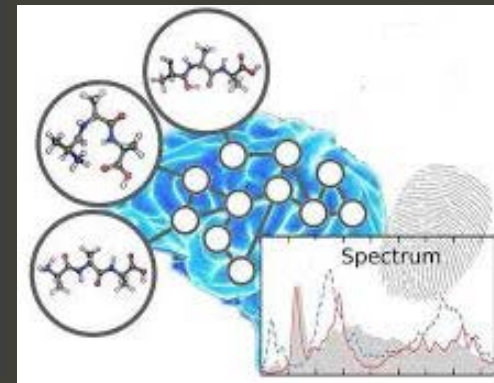
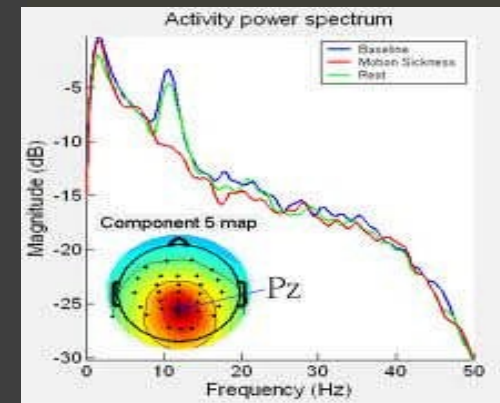
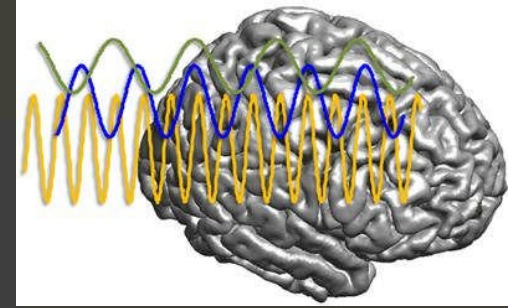
0 - 180 ms 180 - 360 ms 360 - 540 ms 540 - 720 ms

Time ↓

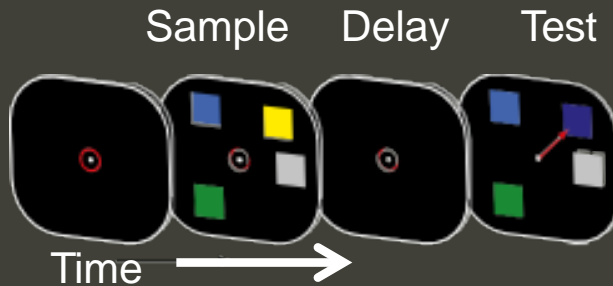
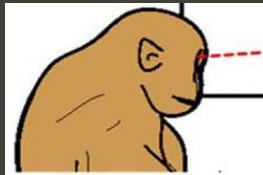
6 8 10 12
Gamma power (σ)

Oscillations

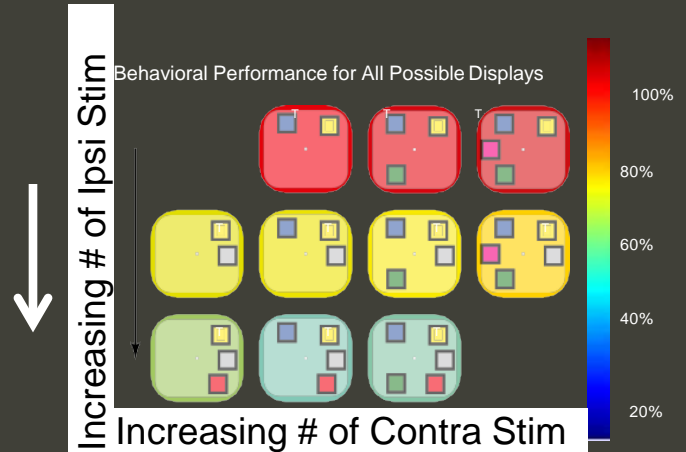
- ✓ Working memory (*Siegel et al. 2009,...*)
- ✓ Visual attention (*Feldman and Friston, 2010,...*)
- ✓ Size, contrast (*e.g. Pinotsis et al., 2014, Pinotsis et al., 2016,...*)
- ✓ Binding Input to cortical representations (*Schoffelen et al., 2005,...*)
- ✓ Information propagation (*e.g. Bastos et al. 2012, Tallon-Baudry et al., 1996...*)
- ✓ Psychiatric diseases, Autism... (*e.g. Uhlhaas and Singer, 2012, Dickinson et al., 2015,...*)



Working Memory Task (Miller Lab, MIT)

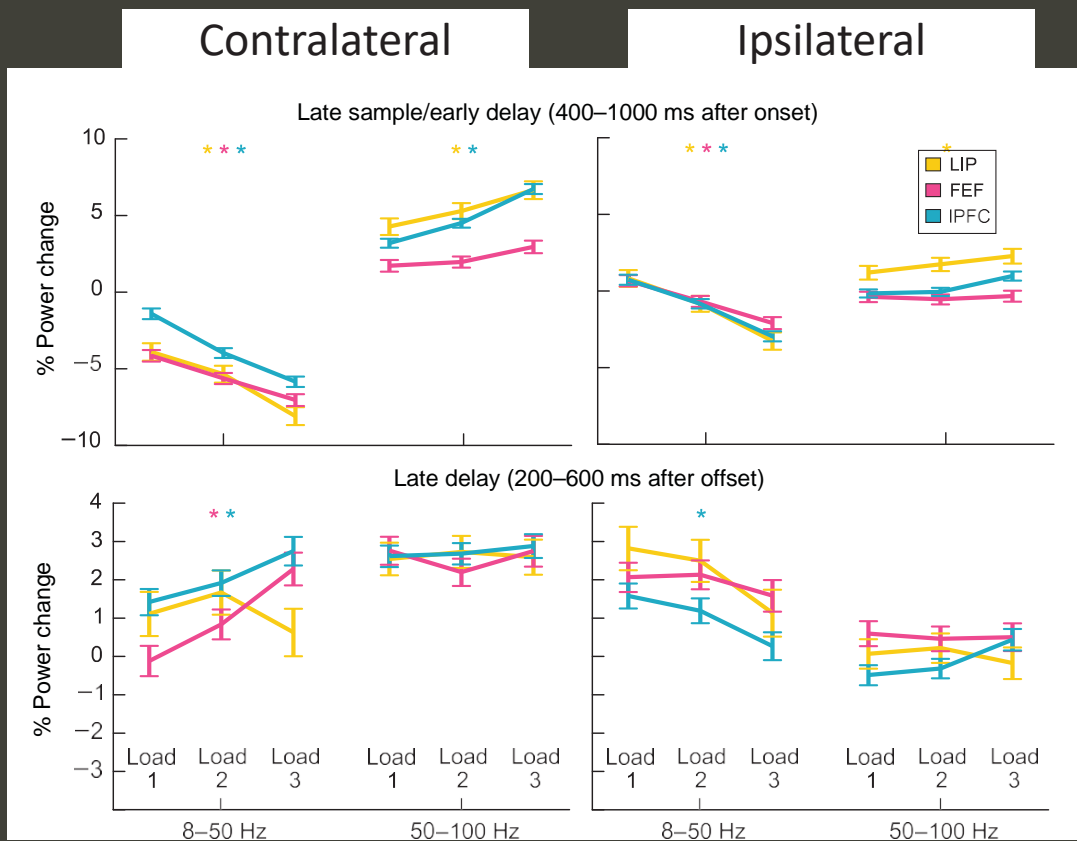


WM performance



When more than 2 items were presented in the same hemifield, the animal's behavioral performance decreased dramatically

Changes in oscillatory power may not yield information directly

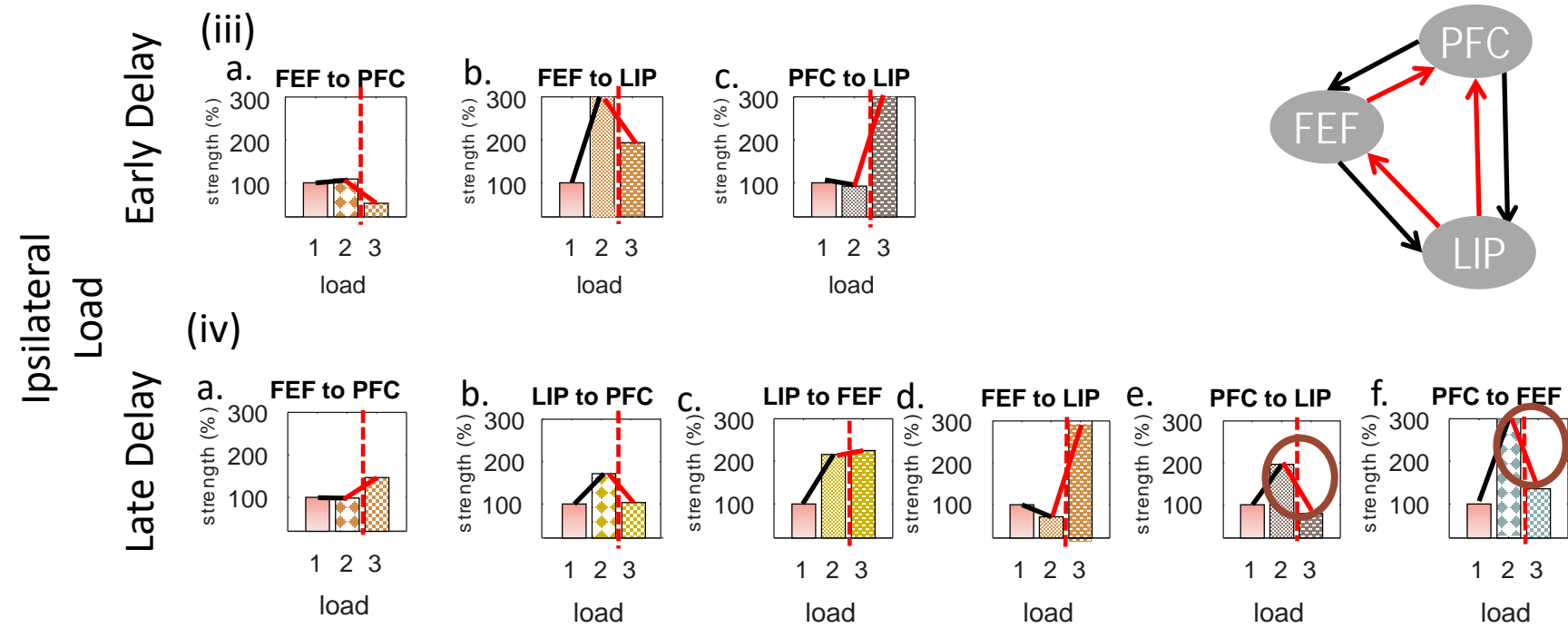


Load effects are weak (1-2% change)

Load effects are similar below and above WM Capacity Limit

→ *Power is **not** informative about the reduction in performance and the mechanisms/network effects resulting in the WM Capacity Limit*

Inferred model connectivity may explain behaviour



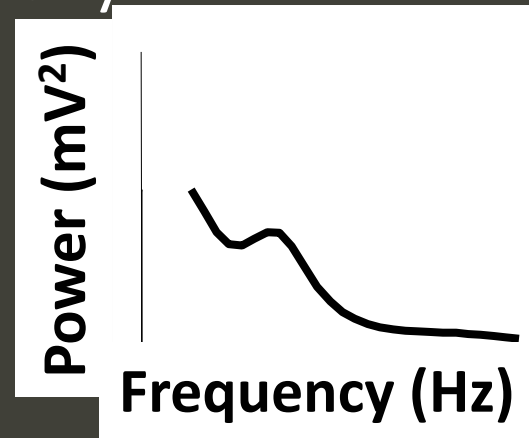
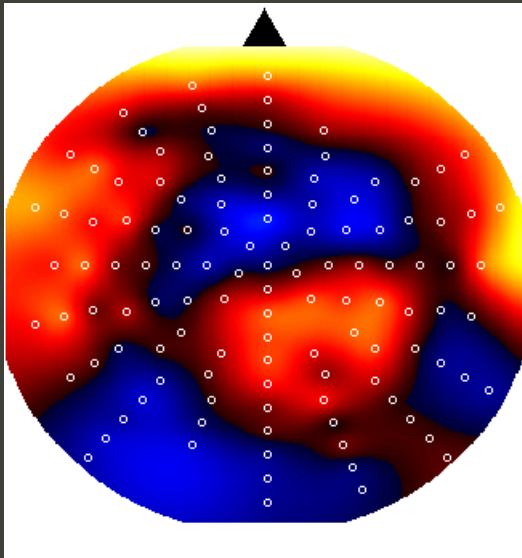
Above capacity – Ipsilateral only where performance is impaired

- *FB from PFC broke down– Could explain reduced performance that load effects on power did not explain.*
- *Predictive Coding model → No predictions from areas that contain memories*
- *No memories → The animal cannot perform the task*

Steps

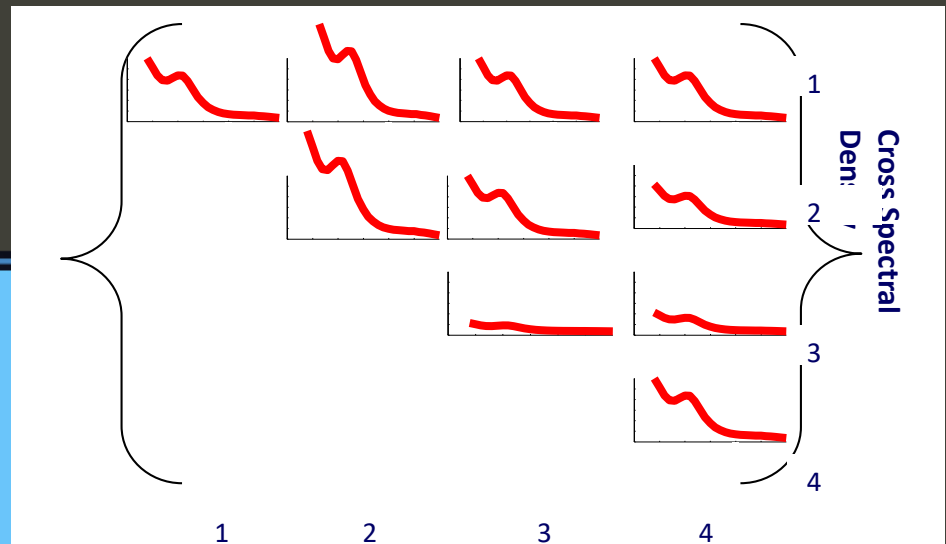
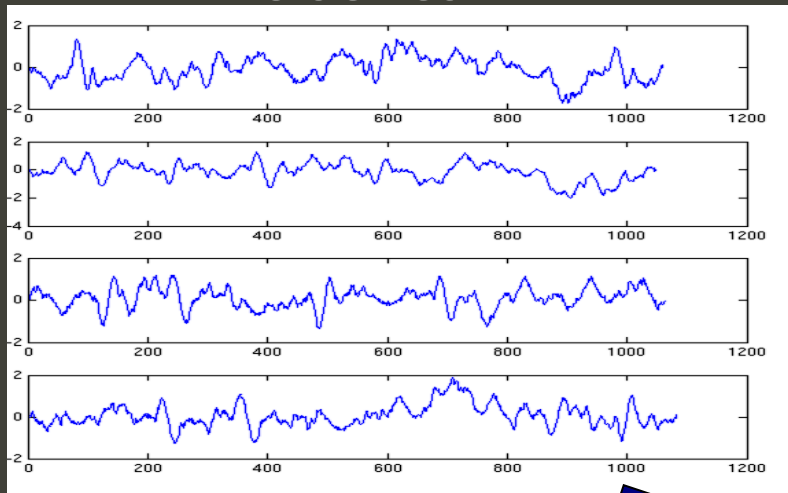


Cross Spectral Density



✓ Summarizes brain response in terms of power at each frequency

EEG - MEG - LFP Time Series

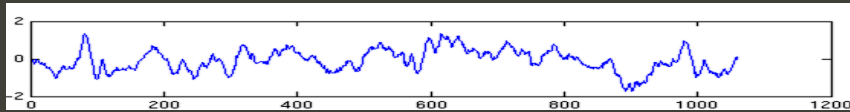


A few LFP channels or EEG/MEG spatial modes

From Time Series to Cross Spectral Densities

Vector Auto-regression p -order model:

Linear prediction formulas that attempt to predict an output $y[n]$ of a system based on the previous outputs



Resulting in a matrices for c Channels

$$H_{ij}(\omega) = \frac{1}{\alpha_1^{ij} e^{i\omega} + \alpha_2^{ij} e^{i\omega^2} + \dots + \alpha_p^{ij} e^{i\omega p}}$$

Cross Spectral Density for channels i, j
at frequencies

$$\omega = 2\pi f$$

$$\left\{ \begin{array}{ccc} g(\omega)_{11} & g(\omega)_{12} & \dots \\ g(\omega)_{12} & \dots & \dots \end{array} \right\}$$

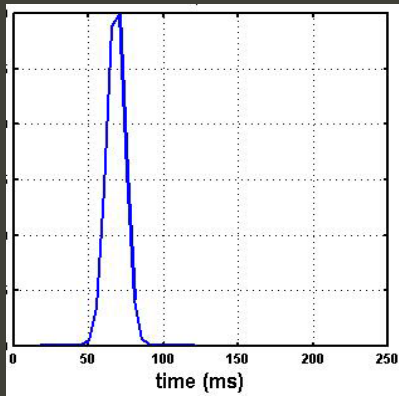
$$y_n = \alpha_1 y_{n-1} + \alpha_2 y_{n-2} \dots + \alpha_p y_{n-p} + e_n$$

$$\{\alpha_{1\dots p} \in A(p) : \{c \times c\}\}$$

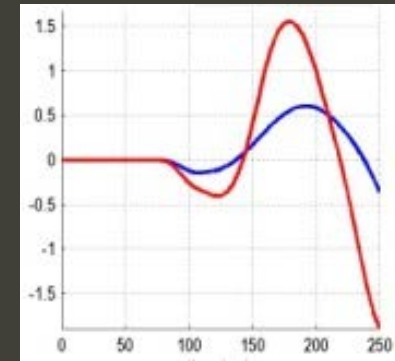
$$g(\omega)_{ij} = f(A(p))$$

$$g(\omega)_{ij} = H_{ij}(\omega) \prod_{ij} H(\omega)_{ij}^*$$

A Brain Area as an Input - Output System



ERP

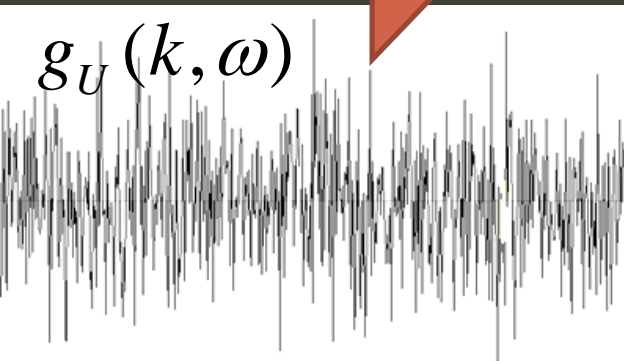


Driving input
or neuronal
innovations

(Model)
Brain region

Predicted
responses ERP
or cross
spectra

$$g_U(k, \omega)$$

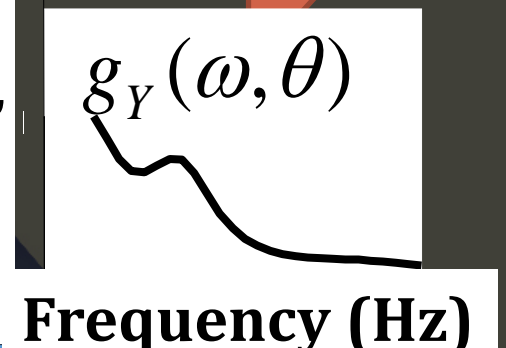


SSR

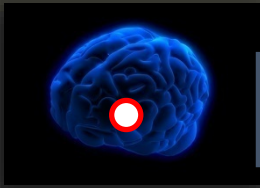
Power (mV^2)

$$g_Y(\omega, \theta)$$

Frequency (Hz)



Same Neural Mass Models as ERP

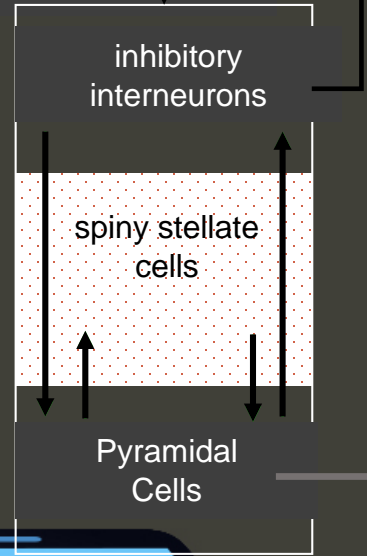


EEG/MEG/LFP signal

Tens of thousands of neurons approximated by their average response. Neural mass models describe the interaction of these averages between populations and sources

neuronal (source) model →

Intrinsic Connections

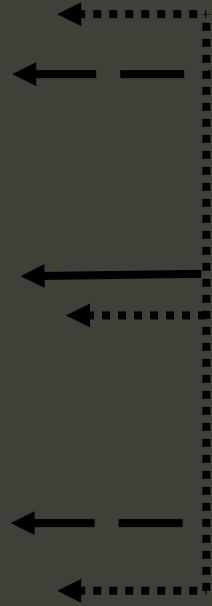


Internal Parameters

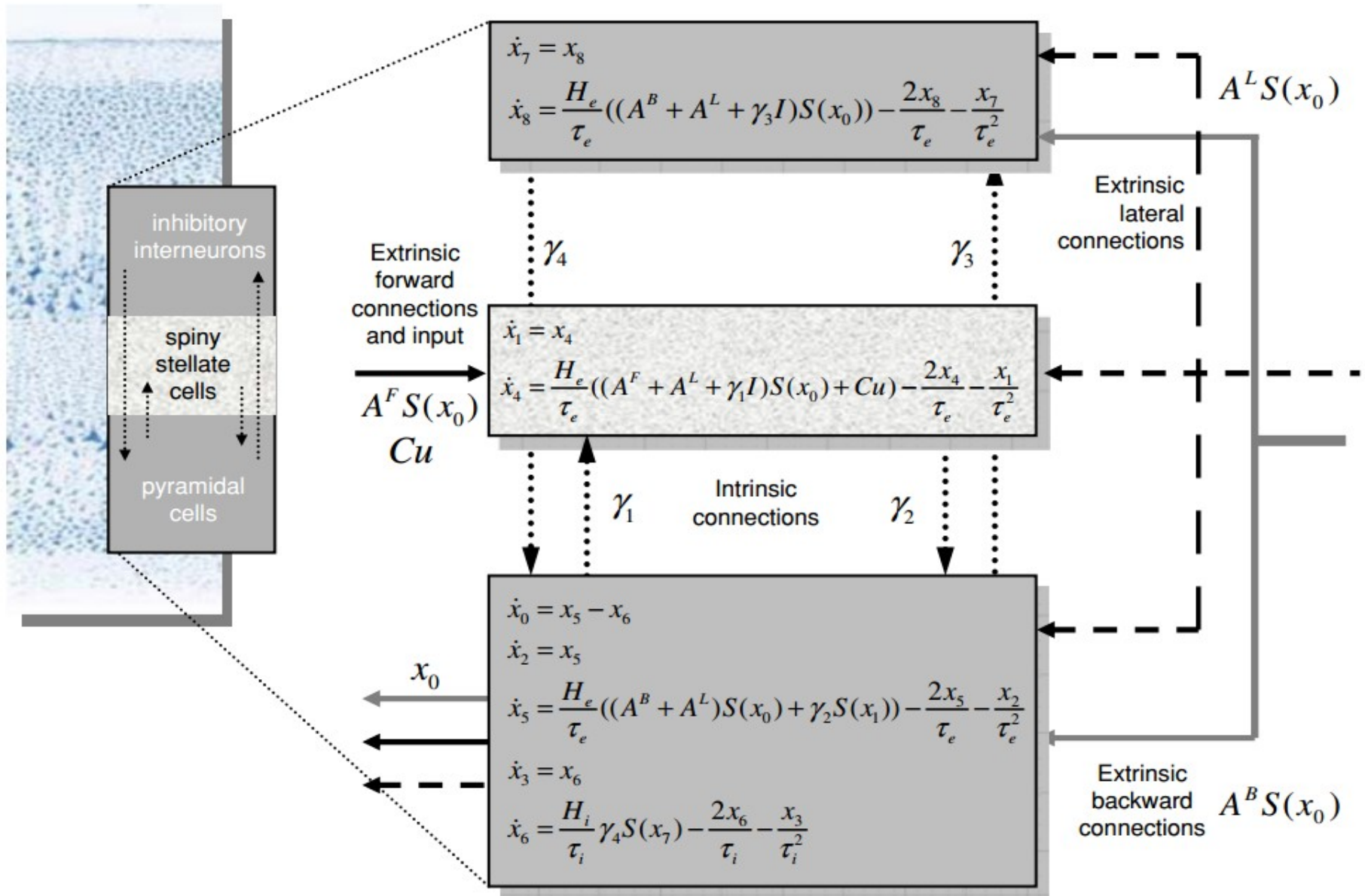
$$\dot{x} = F(x, u, \theta)$$

State equations

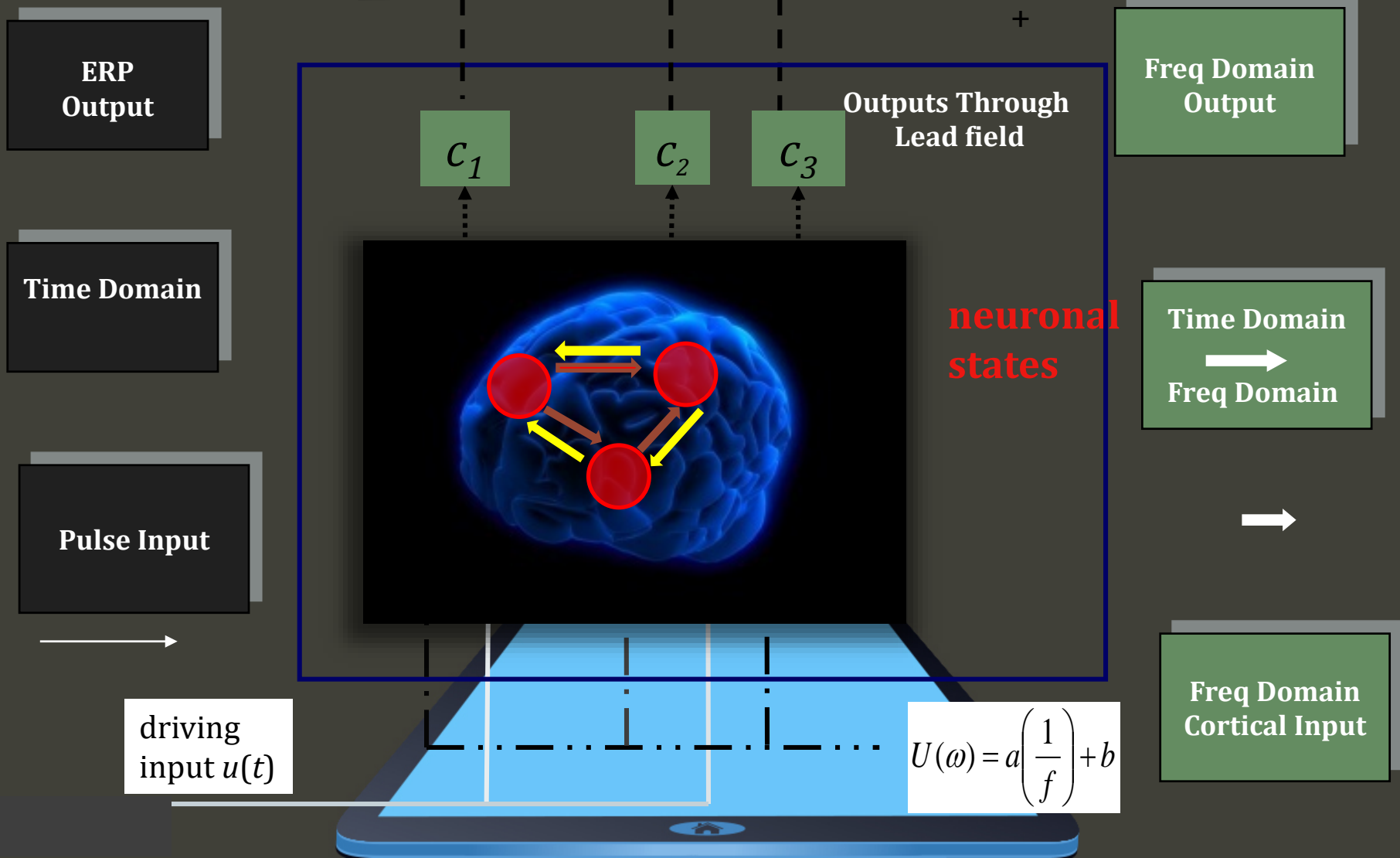
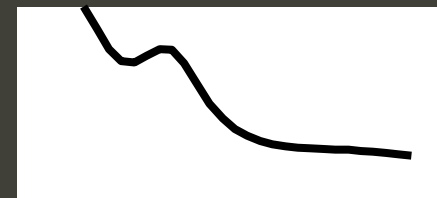
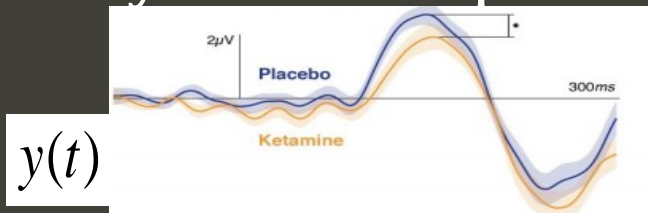
Extrinsic Connections



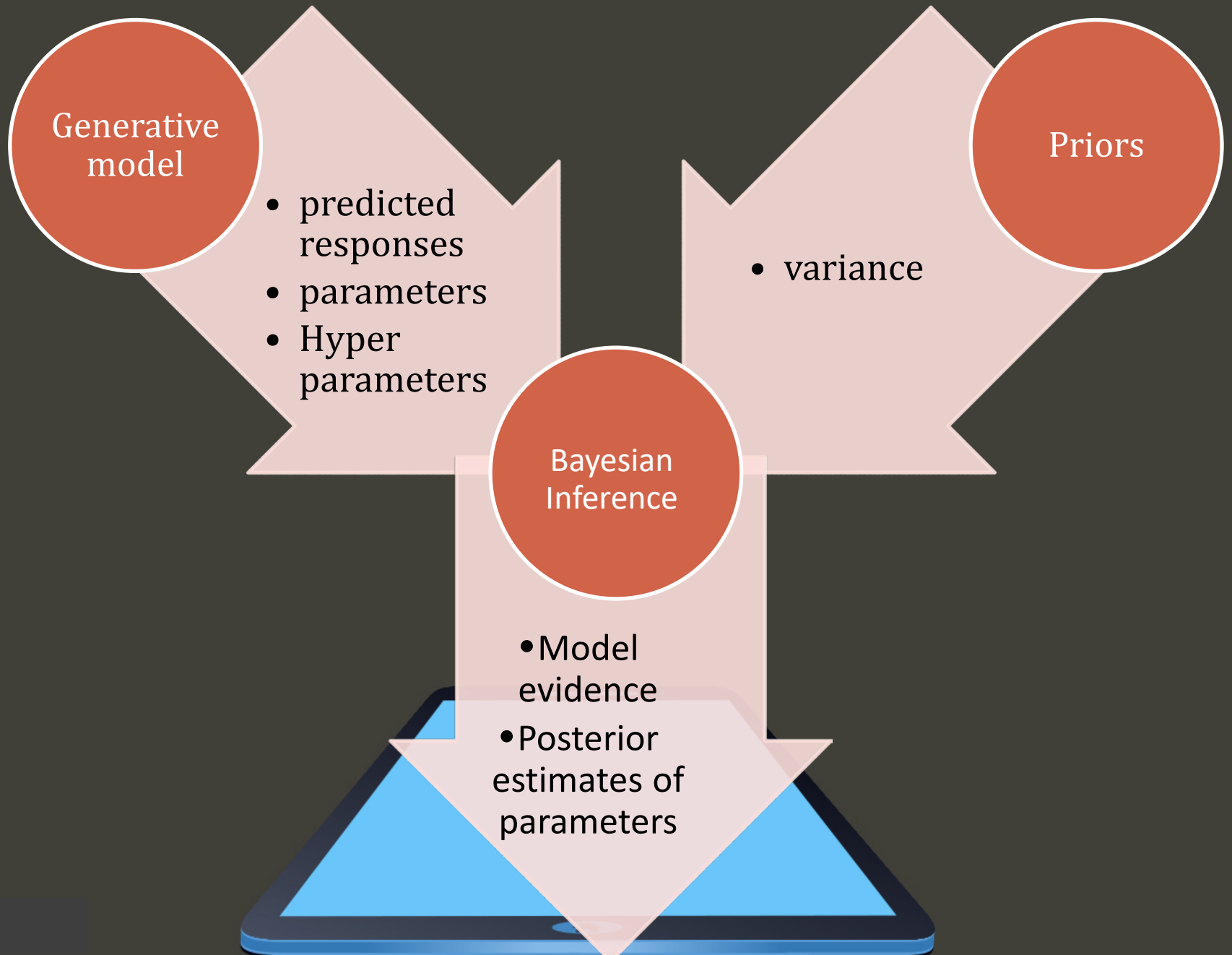
From DCM for ERPs talk in this course (Ryszard Aukstulewicz)



ERP vs Steady State Responses



Roadmap



Bayesian Model Inversion

$$\mathbf{g}_Y(\omega) = g_Y(\omega, \theta) + g_N(\omega, \theta) + \varepsilon(\omega)$$

$$g_N(\omega, \theta) = \alpha_N + \frac{\beta_N}{\omega}$$

$$\text{Re}(\varepsilon) \sim \mathcal{N}(0, \Sigma(\omega, \lambda)) \quad \text{Im}(\varepsilon) \sim \mathcal{N}(0, \Sigma(\omega, \lambda))$$



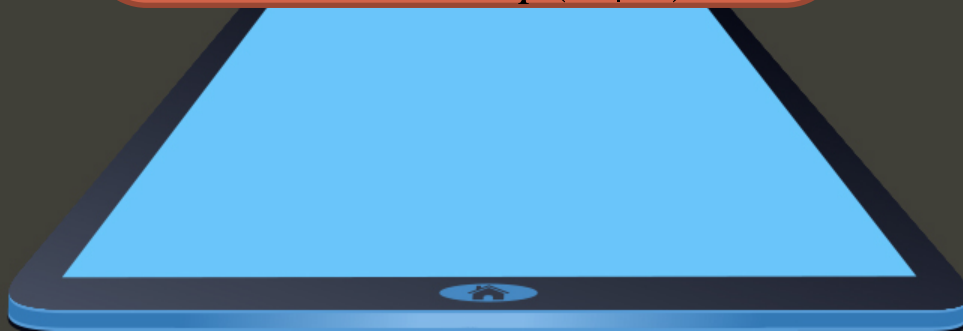
$$p(\theta, m) = N(\mu_\theta, \Sigma_\theta)$$



$$p(G | \theta, m) = N(\mathbf{g}_Y(\omega), \Sigma(\omega, \lambda))$$

$$p(G | m) = \int p(G | \theta, m) p(\theta) d\theta$$

$$p(\theta | G, m) = \frac{p(G | \theta, m) p(\theta, m)}{p(G | m)}$$



Bayesian Model Inversion

Measured data

Specify generative forward model
(with prior distributions of parameters)

Variational Laplace Algorithm

Maximize a free energy bound to model evidence :

$$F = \log p(y|m) - D(q(\theta) \| p(\theta|y,m))$$
$$= \langle \log p(y|\theta, m) \rangle_q - D(q(\theta) \| p(\theta|m))$$

Iterative procedure:

1. Compute model response using current set of parameters and hyperparameters
2. Compare model response with data
3. Improve parameters and hyperparameters

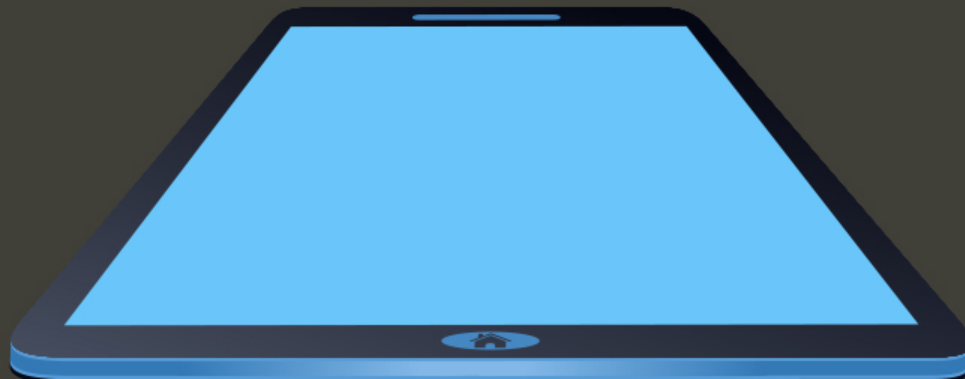
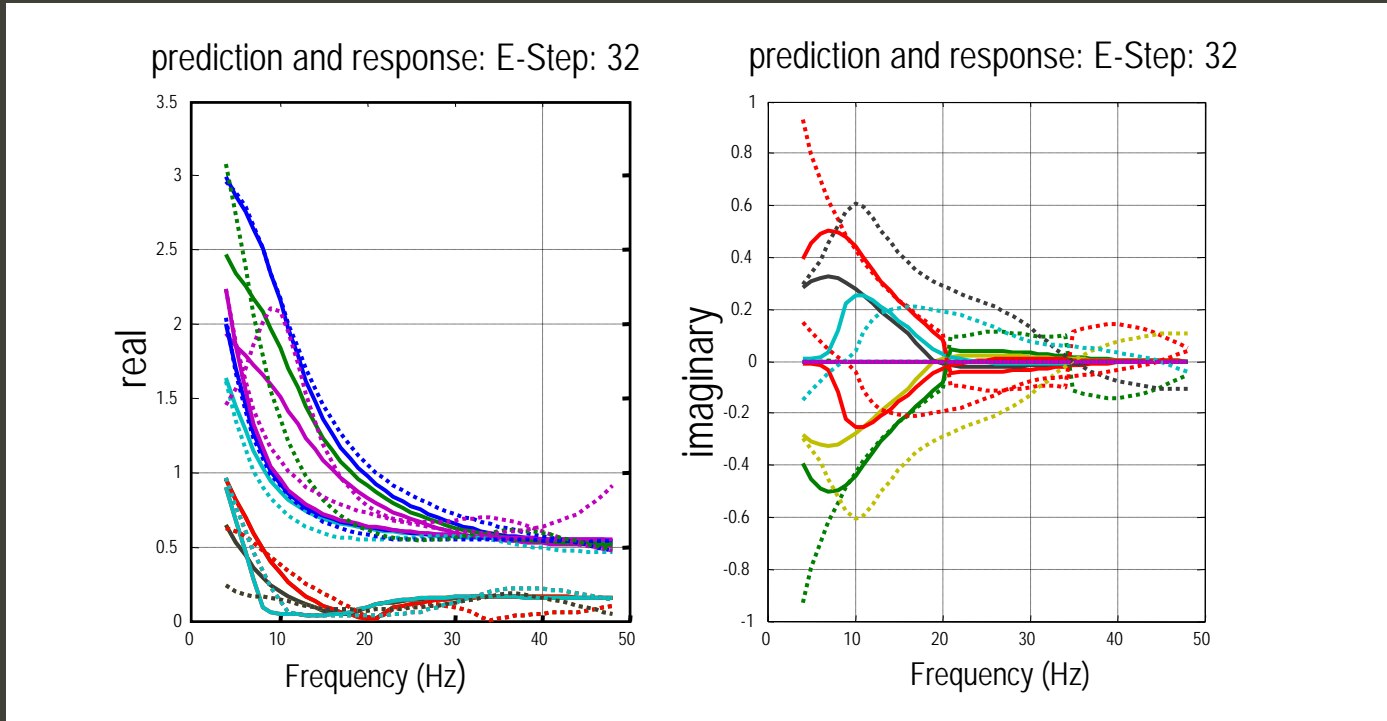
Model comparison via Bayes factor:

$$BF = \frac{p(y | m_1)}{p(y | m_2)}$$

$$q(\theta) \approx p(\theta|y, m)$$

Maximum accuracy over complexity constraints

Data fits have **two** parts: real and imaginary



Example 1: Pharmacological Manipulation of Glutamate and GABA

Question:

- ✓ Are our estimates of excitation and inhibition truthful?

$$H_e, H_i$$

AIM:

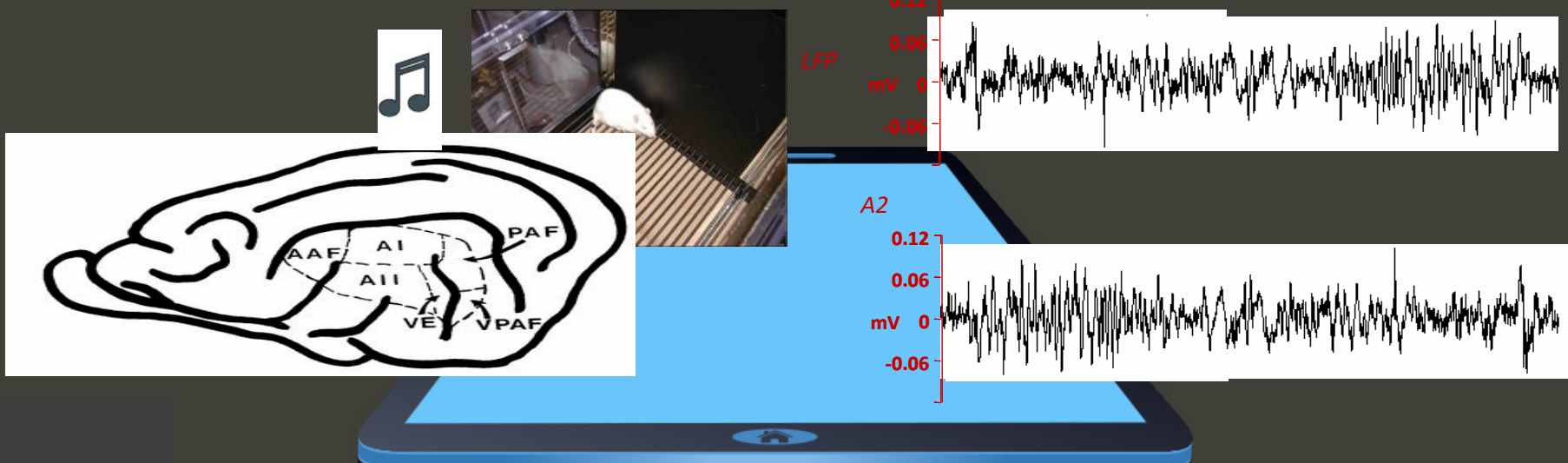
NOT to explain mechanisms of isoflurane BUT
to exploit isoflurane to induce known changes in synaptic
transmission and THEN

- ✓ use LFP recordings and DCM for SSR to infer synaptic changes

Pharmacological Manipulation of Glutamate and GABA

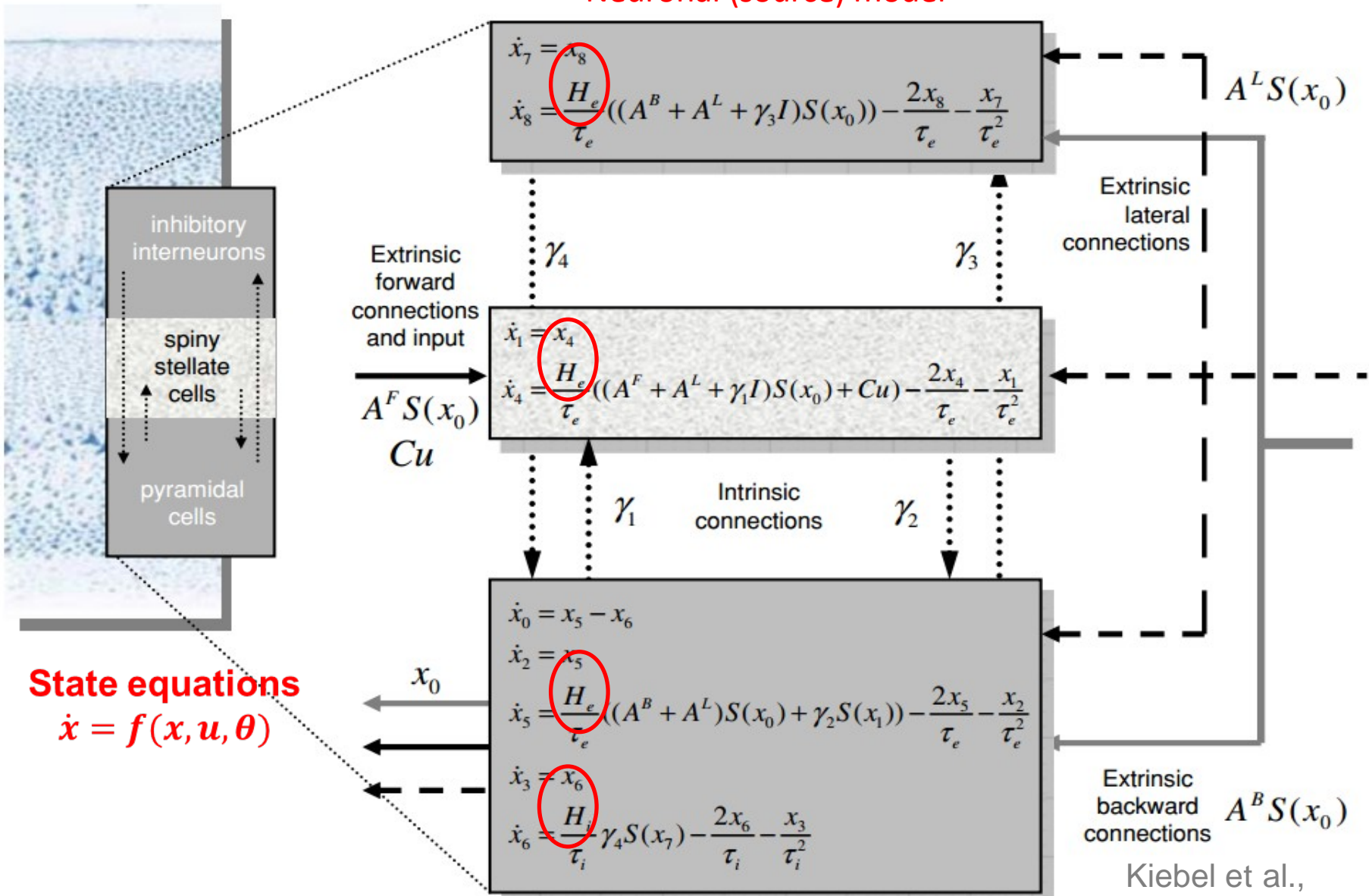
- ✓ Use animal LFP recordings from primary auditory cortex (A1) & posterior auditory field (PAF)
- ✓ Manipulate neurotransmitter processing via anaesthetic agent Isoflurane
- ✓ 4 levels of anaesthesia: each successively decreasing glutamate and increasing GABA (Larsen *et al* Brain Research 1994; Lingamaneni *et al* Anesthesiology 2001; Caraiscos *et al* J Neurosci 2004 ; de Sousa *et al* Anesthesiology 2000
- ✓ White noise stimulus & Silence

1.4 % Isoflurane	1.8 % Isoflurane	2.4 % Isoflurane	2.8 % Isoflurane
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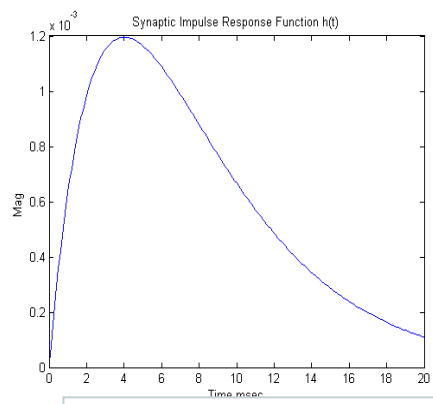
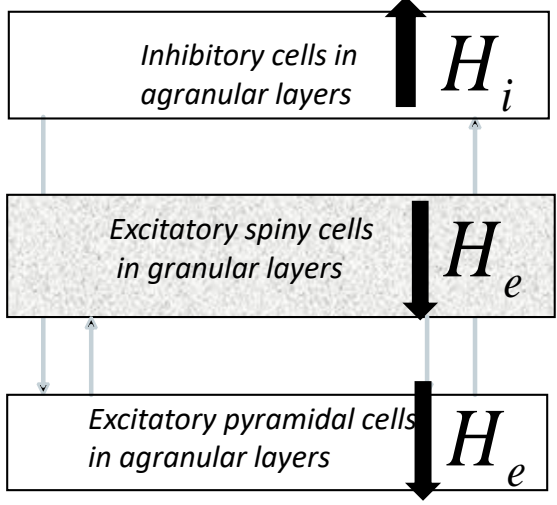
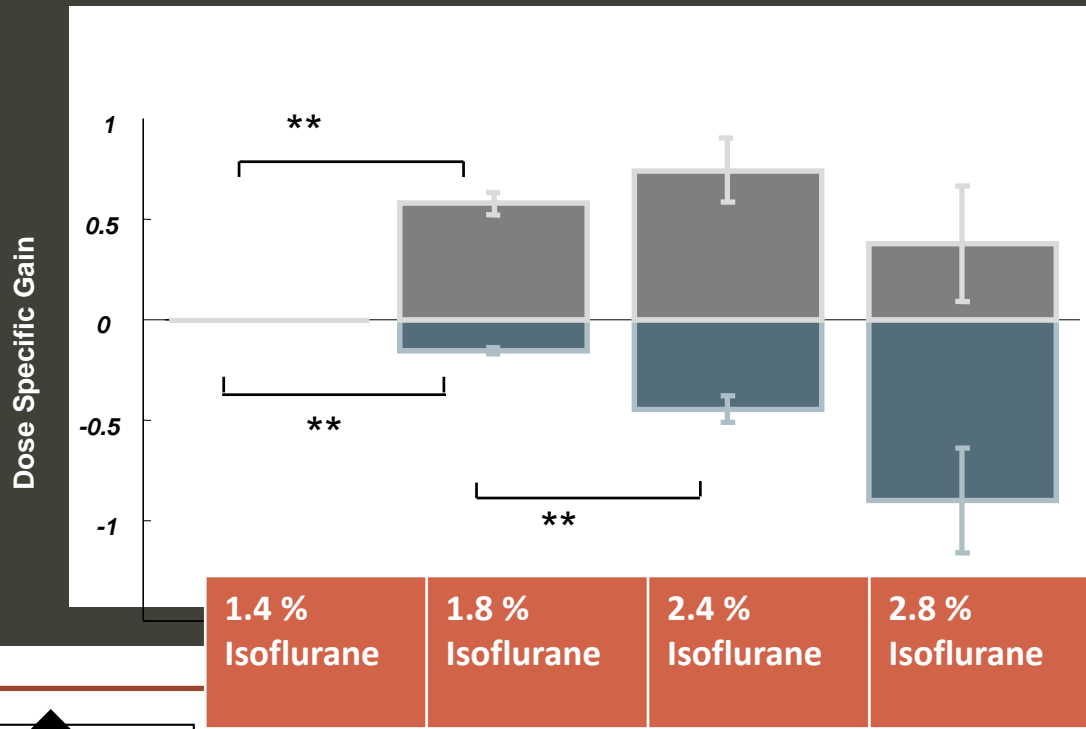
From DCM for ERPs talk in this course

Neuronal (source) model



Pharmacological Manipulation of Glutamate and GABA

Decreased Glutamate Release
Increased gabaergic transmission



Synaptic 'alpha' kernel

Moran et al.,
PLoS ONE, 2011

DCM for SSR recovers known drug-induced changes



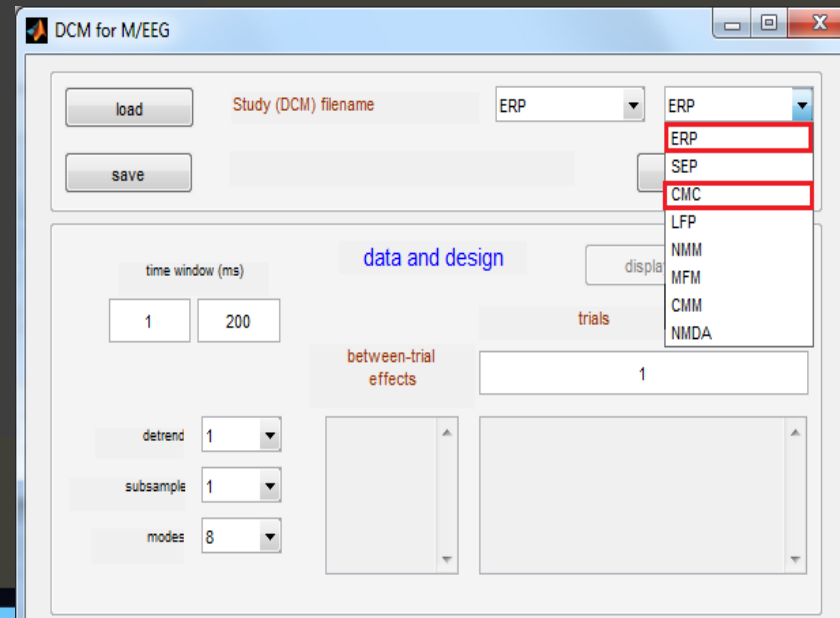
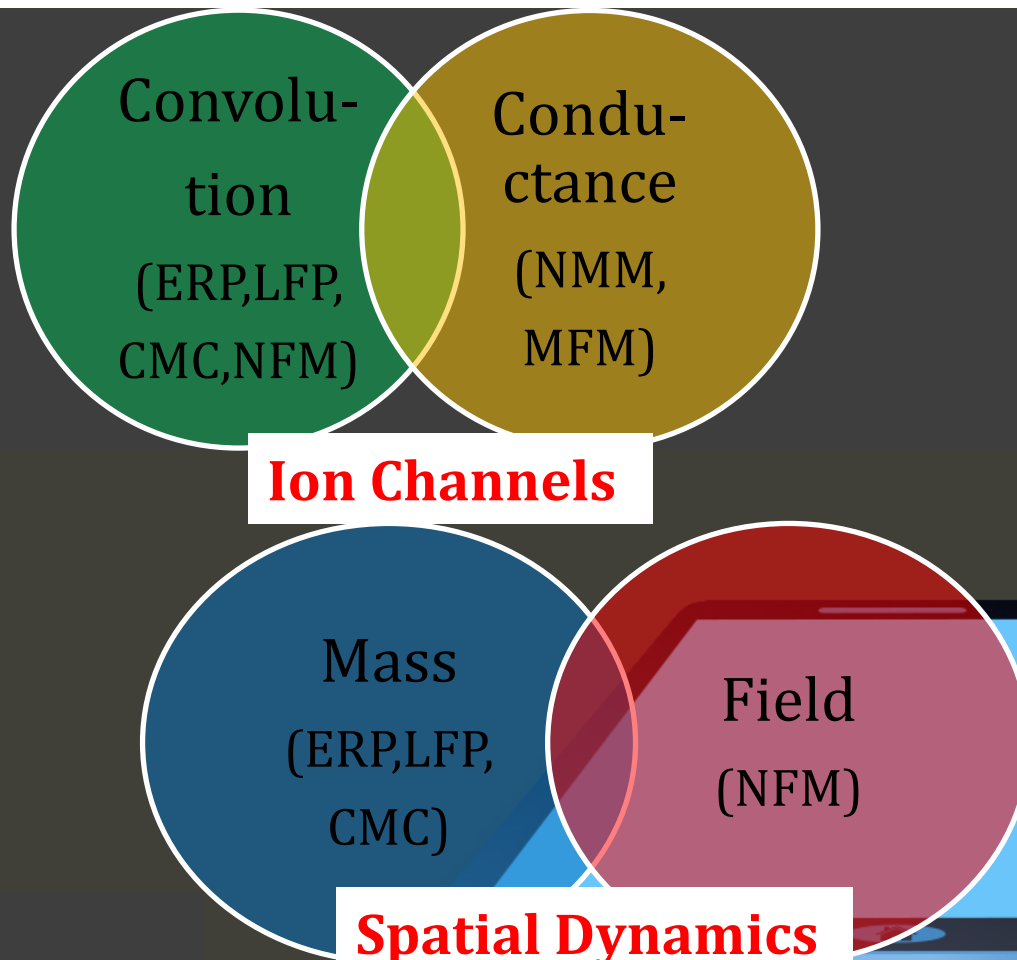
Neural masses and fields in dynamic causal modeling

Rosalyn Moran^{1,2,3*}, Dimitris A. Pinotsis^{1†} and Karl Friston¹

¹ Wellcome Trust Centre for Neuroimaging, Institute of Neurology, University College London, London, UK

² Virginia Tech Carilion Research Institute, Virginia Tech, Roanoke, VA, USA

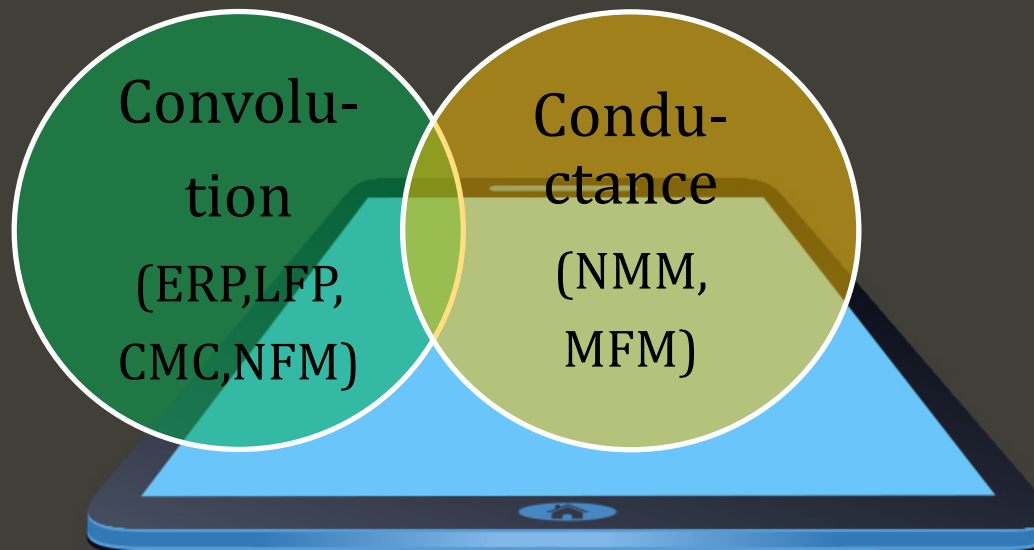
³ Bradley Department of Electrical and Computer Engineering, Virginia Tech, Blacksburg, VA, USA



Taxonomy - I

With or Without Ion Channels ?

- Characterize nonlinear synaptic transmission or linear convolution effects.
- Explain the relation between channel-specific conductances and observed cortical responses.

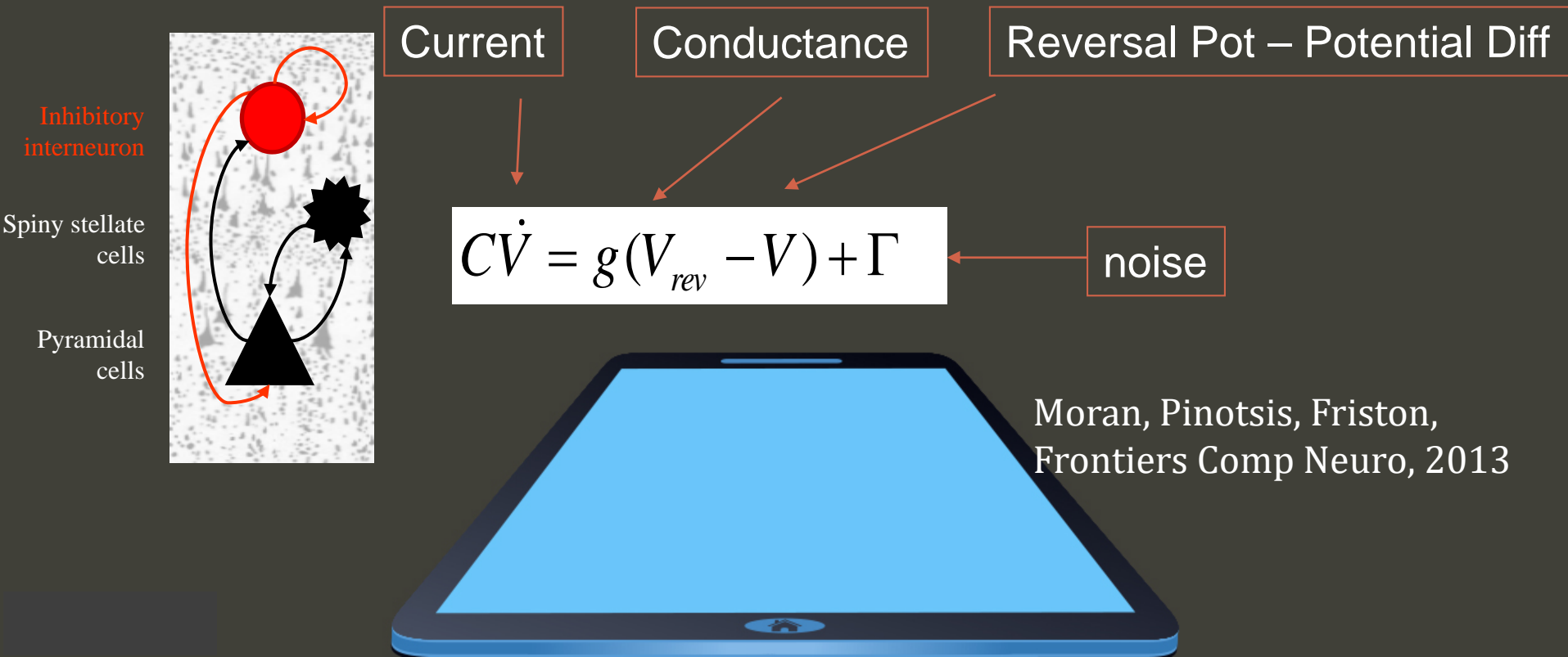


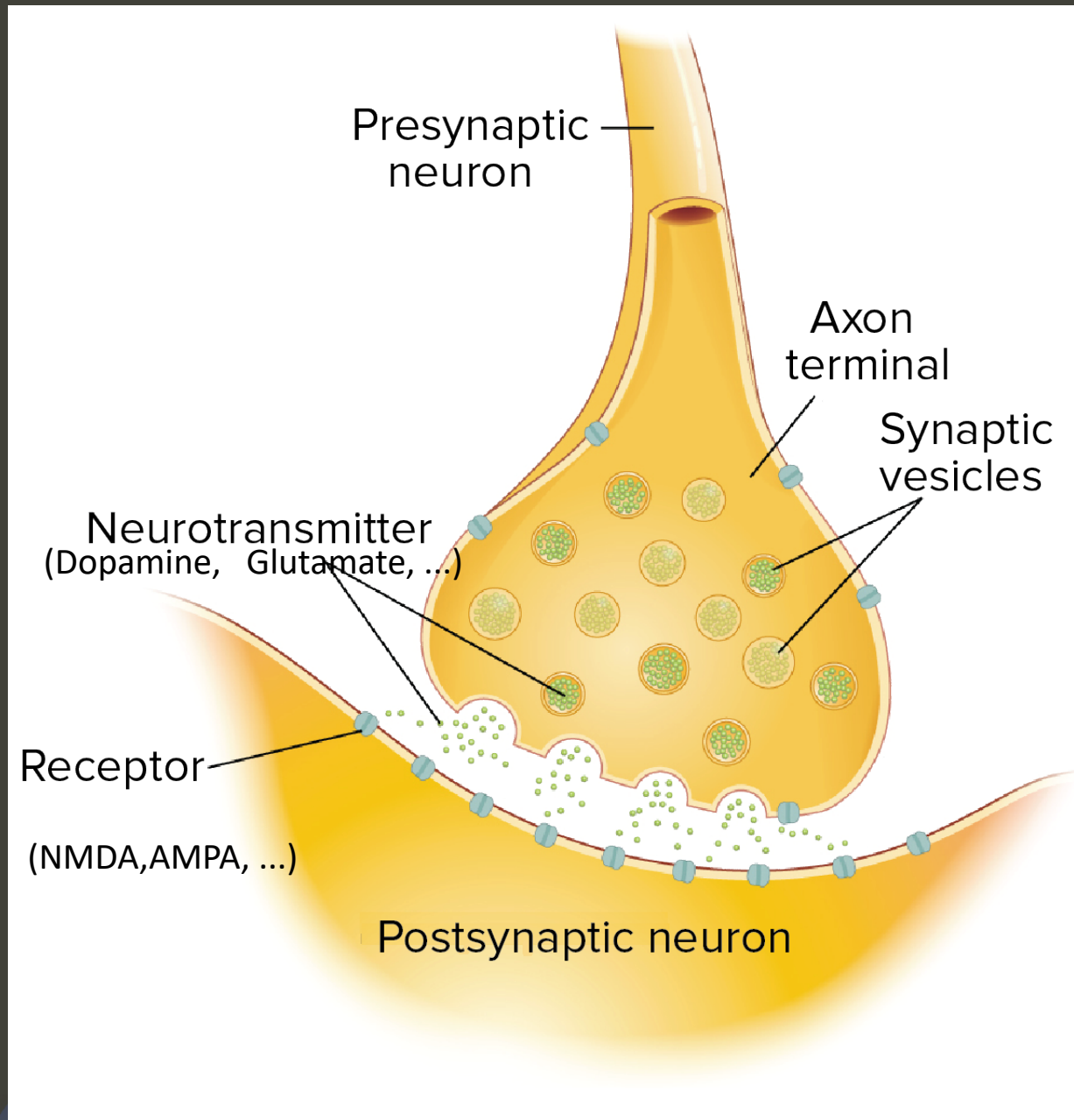
Conductance-based Mass Model

- ✓ More realistic parameterization of synaptic currents
- ✓ Same architecture
- ✓ A capacitor stores electric charges
- ✓ Neuronal population as a capacitor
- ✓ $g=1/R$
- ✓ $V=IR$ (Ohms law) or
 $V=I/g$ or
 $gV=I$

$$q(t) = CV(t)$$

$$I(t) = CV(\dot{t})$$





Connectivity

$$\dot{g}(t) = \kappa [\gamma \sigma(V(t)) - g(t)]$$

Conductance

Time Constant

Afferent Firing

No. open channels

- ✓ Response of each population is determined by a set of synaptic **time constants** corresponding to opening and closing of channels and receptors
- ✓ Predicted dynamics are defined over these timescales and non-linear interaction between membrane potential and conductance

Pinotsis et al., Frontiers
Comp Neuro, 2013



Losing Control Under Ketamine: Suppressed Cortico-Hippocampal Drive Following Acute Ketamine in Rats

1
1

Rosalyn J Moran^{*,1,2,6}, Matthew W Jones^{3,6}, Anthony J Blockeel³, Rick A Adams², Klaas E Stephan^{2,4,5} and Karl J Friston²

Neural state equations

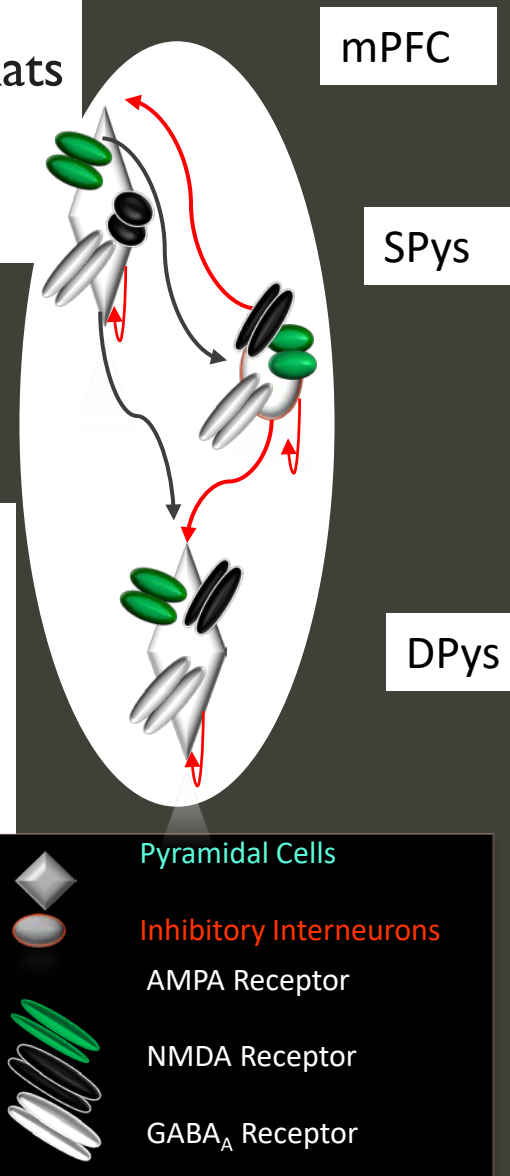
$$C\dot{V} = g_{Na}(V_{Na} - V) + g_{Ca}f_{MG}(V_{Ca} - V) + g_{Cl}(V_{Cl} - V) + \Gamma$$

$$\dot{g}_{Na} = \kappa_{AMPA}(\gamma_{ec}\sigma - g_{Na}) - \text{Sodium}$$

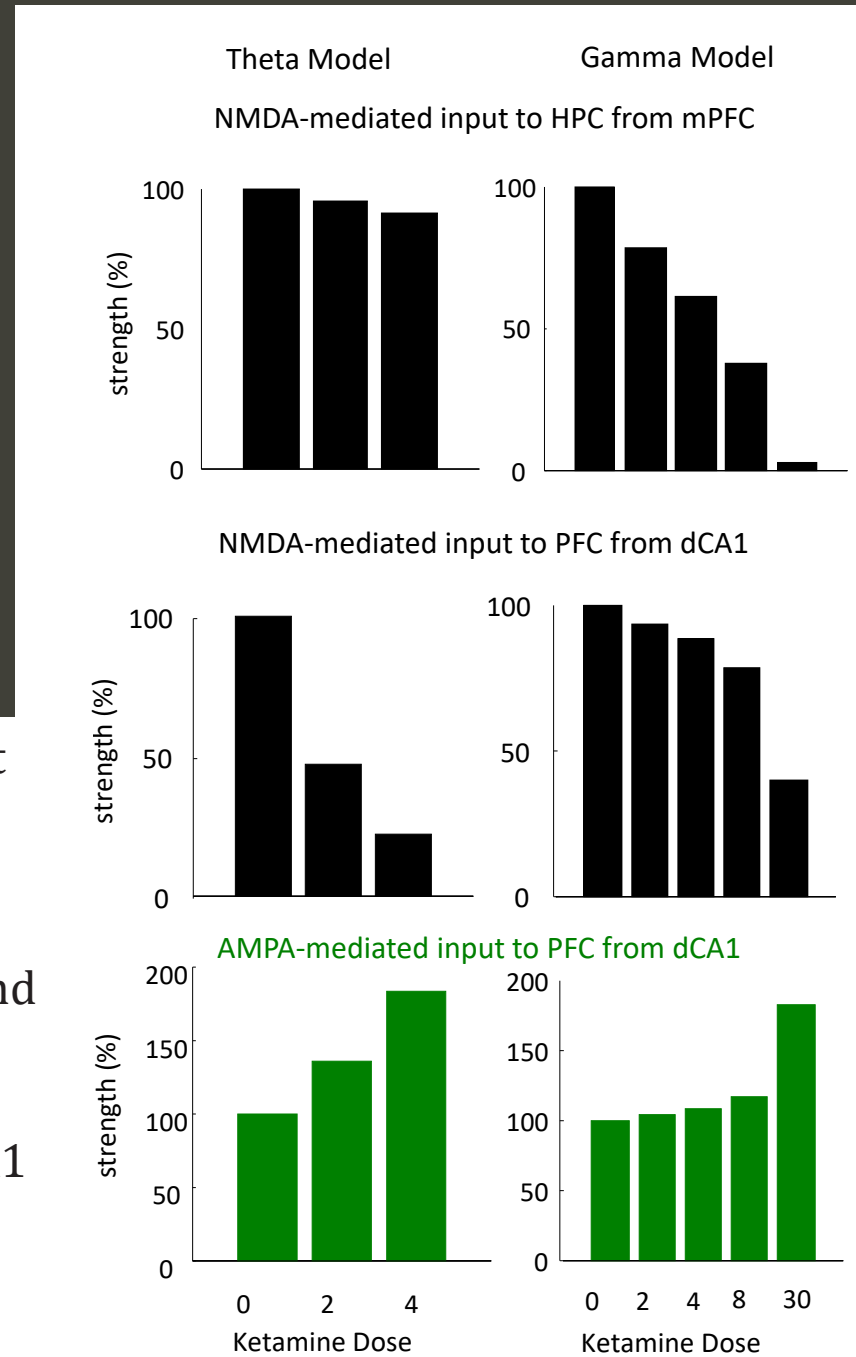
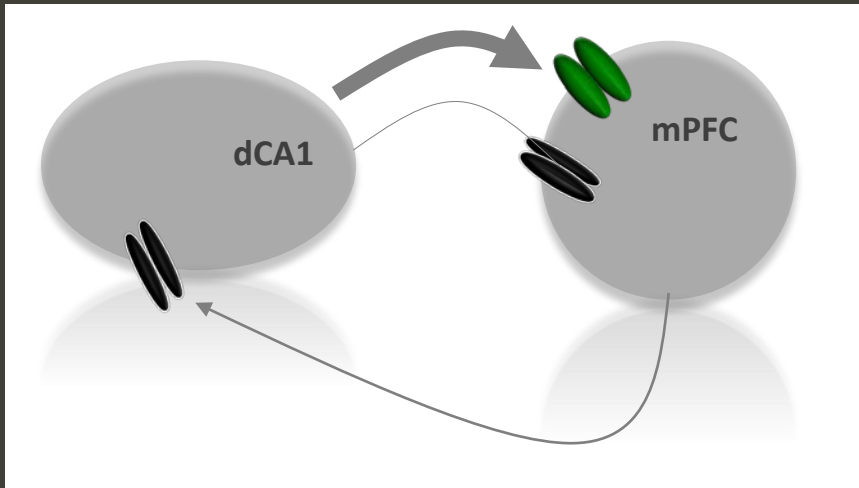
$$\dot{g}_{Cl} = \kappa_{GABA}(\gamma_{ii}\sigma - g_{Cl}) - \text{Chlorine}$$

$$\dot{g}_{Ca} = \kappa_{NMDA}(\gamma_{ec}\sigma - g_{Ca}) - \text{Calcium}$$

Theta reduction in the hippocampus and Gamma enhancement in hippocampus and neocortex.



Connectivity changes under Ketamine

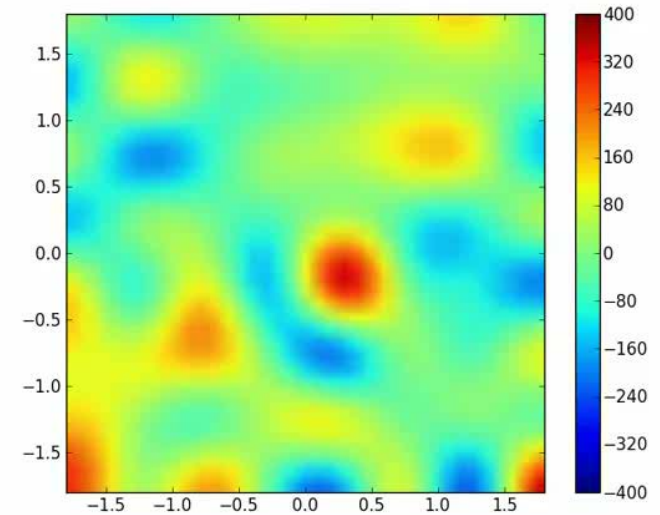


- ✓ Parametric effects of ketamine were consistent across theta and gamma ranges
- ✓ NMDAR-mediated responses decreased parametrically with dose from HPC to mPFC and from mPFC to HPC
- ✓ AMPAR-mediated forward connection from CA1 to mPFC increased with dose

Taxonomy - II

With or Without Spatial Dynamics ?

- ✓ Characterize point or spatially extended neuronal processes
- ✓ Explain the relation between temporal or spatiotemporal properties of cortical sources and observed brain dynamics



Mass
(ERP, LFP,
CMC)

Field
(NFM)



Wave equations describing propagation of afferent input between points on the cortex and equations for voltages

Inhibitory cells in supragranular layers

$$\ddot{v}_2 + 2\kappa_i \dot{v}_2 + \kappa_i^2 v_2 = \kappa_i m_i \mu_2$$

$$\ddot{\mu}_2 + 2sc_{23} \dot{\mu}_2 - s^2 (\mu_{2,xx} - c_{23}^2 \mu_2) = \alpha_{23} (s^2 c_{23} \sigma(v_3) + s \dot{\sigma}(v_3))$$

a_{32}, c_{32}

a_{23}, c_{23}

$U(t)$ → Excitatory spiny cells in granular layers

$$\ddot{v}_1 + 2\kappa_e \dot{v}_1 + \kappa_e^2 v_1 = \kappa_e m_e (\mu_1 + U)$$

$$\ddot{\mu}_1 + 2sc_{13} \dot{\mu}_1 - s^2 (\mu_{1,xx} - c_{13}^2 \mu_1) = \alpha_{13} (s^2 c_{13} \sigma(v_3) + s \dot{\sigma}(v_3))$$

a_{13}, c_{13}

a_{31}, c_{31}

s conduction velocity

Excitatory pyramidal cells in supra- and infragranular layers

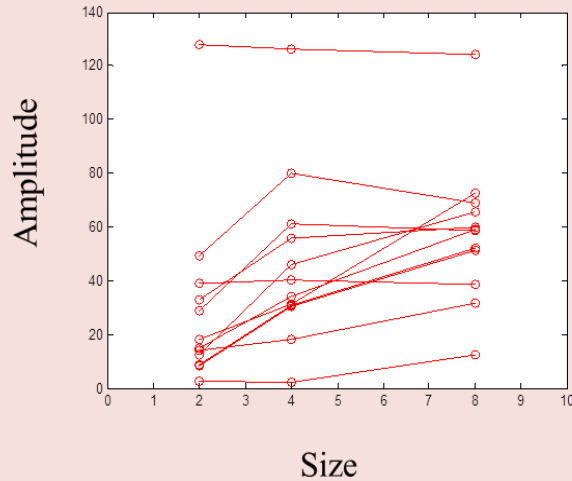
$$\ddot{v}_3 + 2\kappa_e \dot{v}_3 + \kappa_e^2 v_3 = \kappa_e m_e \mu_3$$

$$\ddot{\mu}_3 + 2sc_{31} \dot{\mu}_3 - s^2 (\mu_{3,xx} - c_{31}^2 \mu_3) = \alpha_{31} (s^2 c_{31} (\sigma(v_1) - \sigma(v_2)) + s (\dot{\sigma}(v_1) - \dot{\sigma}(v_2)))$$

$$\dot{V} = -BV + D \otimes F \circ V + U$$

LFP signal

Size induced intersubject variability of amplitude of visually induced gamma oscillations



$$\ln p(g(\omega), \theta^{(1)}, \theta^{(2)}) = \sum_i \ln p(g(\omega)_i | \theta^{(1)}) + \ln p(\theta^{(1)} | \theta^{(2)}) + \ln p(\theta^{(2)})$$

$$p(g(\omega)_i | \theta^{(1)}) = \mathcal{N}(\Gamma_i(\theta^{(1)}), \Sigma_i(\theta^{(1)}))$$

$$p(\theta^{(1)} | \theta^{(2)}) = \mathcal{N}(\Gamma(\theta^{(2)}), \Sigma(\theta^{(2)}))$$

$$p(\theta^{(2)}) = \mathcal{N}(\eta, \Sigma)$$

$$\theta^{(1)} = (X \otimes I)\theta^{(2)} + \varepsilon^{(2)}$$

$$\theta^{(2)} = \eta + \varepsilon^{(3)}$$

$$g_{lm}(\omega) = \hat{g}_{lm}(\omega) + g_n(\omega) + \varepsilon^{(1)}$$

$$\hat{g}_{lm}(\omega) = \sum_k T_l(k, \omega) g_u(k, \omega) T_m(k, \omega)^\dagger$$

$$T_q(k, \omega) = L_q(k, \varphi) Q \cdot T(k, \omega, \theta^{(1)})$$

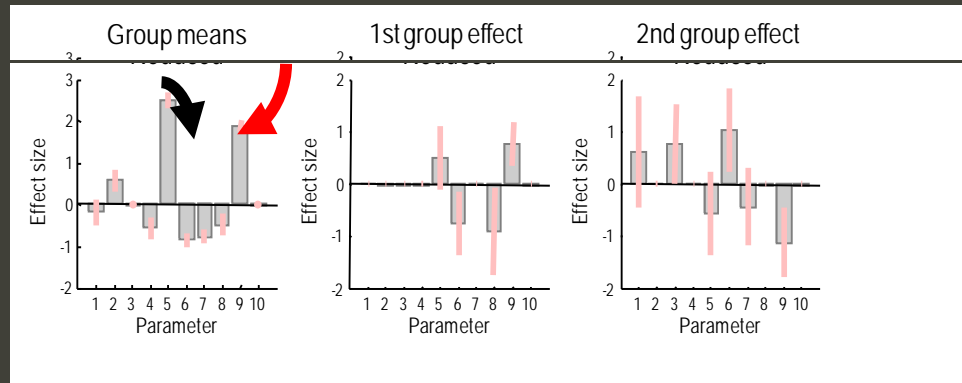
$$g_n(\omega) = \alpha_n + \beta_n / \omega$$

$$g_u(\omega) = \alpha_u + \beta_u / \omega$$

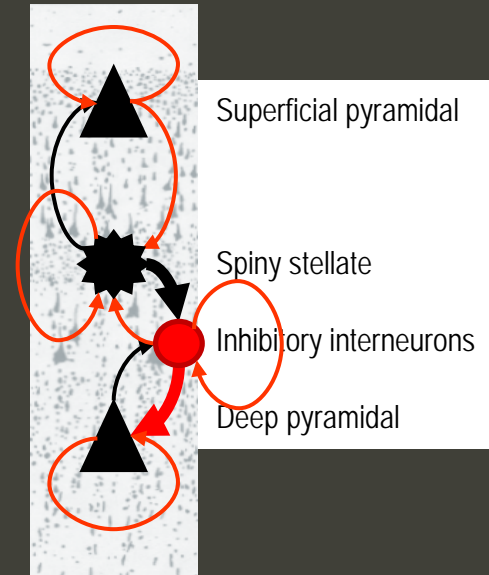
$$\text{Re}(\varepsilon^{(1)}) \sim \mathcal{N}(0, \Sigma(\omega, \lambda)) \quad \text{Im}(\varepsilon^{(1)}) \sim \mathcal{N}(0, \Sigma(\omega, \lambda))$$

- ✓ Gamma oscillations important for visual perception and affected by stimulus properties
- ✓ Gamma amplitude increases with size, cf. surround suppression, figure background segmentation, contour integration... (Super et al, 2010, Hess...)
- ✓ Either linear increase or saturation with size
- ✓ What determines an individual's spectral response?

Individual differences in oscillatory power reveal commonalities and differences across subjects



Posterior estimates for 2nd level parameters

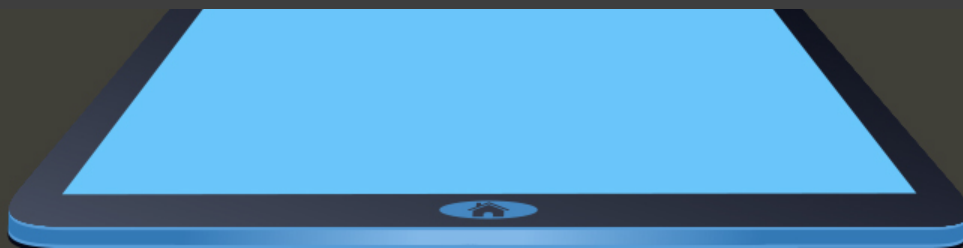


- ✓ Microscopic estimates of cortical function and structure obtained non-invasively
- ✓ Amplitude differences over subject best explained by individual differences in the intrinsic connectivity to and from inhibitory interneurons
- ✓ This reflects differences in the excitation to inhibition balance
- ✓ In accord with PC where size effects are mediated by differences in cortical excitability
- ✓ ...and PING networks:
local inhibition drives gamma oscillations

Pinotsis et al.,
Human Brain Mapping, 2016

Summary

- ✓ DCM is a generic framework for asking mechanistic questions based on neuroimaging data (e.g. drug-induced changes in the balance of synaptic transmission)
- ✓ Neural mass models parameterise intrinsic and extrinsic ensemble connections and synaptic measures (time constants, effective connectivity, neuromodulation...)
- ✓ DCM for SSR provides a compact characterisation of multi- channel LFP or M/EEG data in the frequency domain
- ✓ Bayesian inversion provides parameter estimates and allows model comparison for competing hypothesised architectures
- ✓ DCM for SSR uses power spectra to make inferences about hidden neuronal states and parameter. It has been validated using simulations, pharmacological interventions and developmental manipulations



Thanks to

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Rick Adams

Ryszard Auksztulewicz

Gareth Barnes

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